

Shift 2 Left

Shift up 1

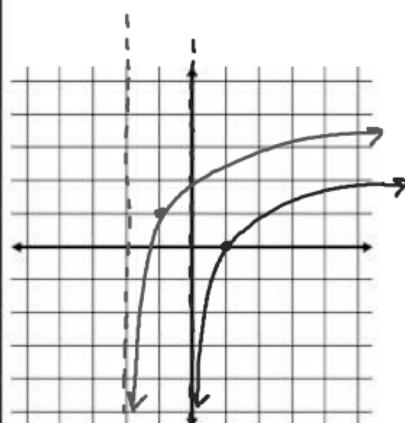
Describe how to transform the graph of $y = \ln x$ into the graph of the given function. Sketch the graph by hand.

$$\ln(-x+3)$$

a) $g(x) = \ln(\underline{x+2}) + 1$

b) $h(x) = \ln(3-x)$

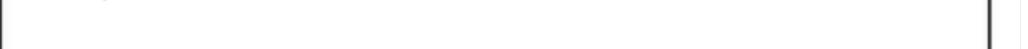
$$\ln - (x-3)$$



1) Determine the vertical asymptotes

$$x = -1.63$$

2) Determine the x-intercept



1) Determine the vertical asymptotes

$$x = 3$$

2) Determine the x-intercept

$$x = 2$$

3) Determine the domain and range

$$D: (-\infty, 3)$$

$$R: (-\infty, \infty)$$

4) Intervals of Increase or Decrease

$$\text{Dec } (-\infty, 3)$$

5) Determine the end behavior

$$\lim_{x \rightarrow -\infty} f(x) = \infty \quad \lim_{x \rightarrow 3^-} f(x) = -\infty$$

6) Intervals of Concavity

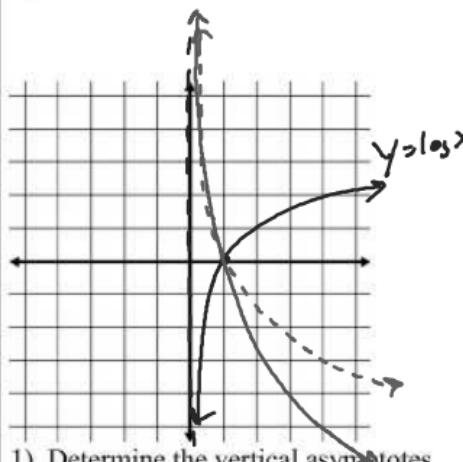
$$\text{Concave Down } (-\infty, 3)$$

$$\lim_{x \rightarrow -2^+}$$

Reflection
over x-axis
Vertical Stretch
by factor of 3

Describe how to transform the graph of $y = \log x$ into the graph of the given function. Sketch the graph by hand.

a) $g(x) = -3\log x$



- 1) Determine the vertical asymptotes

$$x = 0$$

- 2) Determine the x-intercept

$$x = 1$$

- 3) Determine the domain and range

$$D: (0, \infty)$$

$$R: (-\infty, \infty)$$

- 4) Intervals of Increase or Decrease

$$\text{Dec } (0, \infty)$$

- 5) Determine the end behavior

$$\lim_{x \rightarrow \infty} f(x) = -\infty \quad \lim_{x \rightarrow 0^+} f(x) = \infty$$

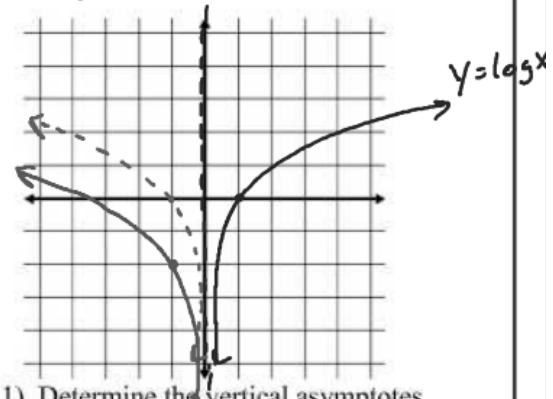
- 6) Intervals of Concavity

$$\text{Concave up } (0, \infty)$$

$\log x$

b) $h(x) = \log(-x) - 2$

Reflect over y-axis
Shift Down 2



- 1) Determine the vertical asymptotes

$$x = 0$$

- 2) Determine the x-intercept

$$(-100, 0)$$

- 3) Determine the domain and range

$$D: (-\infty, 0)$$

$$R: (-\infty, \infty)$$

- 4) Intervals of Increase or Decrease

$$\text{Dec } (-\infty, 0)$$

- 5) Determine the end behavior

$$\lim_{x \rightarrow -\infty} f(x) = \infty \quad \lim_{x \rightarrow 0^-} f(x) = -\infty$$

- 6) Intervals of Concavity

$$\text{Concave } (-\infty, 0)$$

VL Due Friday

4.3

11 pm

$$g(x) = \ln(x+2) + 1$$

$$h(x) = \log(-x) - 2$$

4.4

$$0 = \ln(x+2) + 1$$

$$0 = \log(-x) - 2$$

$$-1 = \ln(x+2)$$

$$2 = \log(-x)$$

$$e^{-1} = x+2$$

$$-x = 10^2$$

$$x = e^{-1} - 2$$

$$-x = 100$$

$$x = -100$$

Chapter 3: Exponential, Logistic, and Logarithmic Functions
3.4: Properties of Logarithmic Functions

What you'll Learn About

Use your Calculator to Determine which of the following are True.

1. $\log(5+2) = \log 5 + \log 2$ 2. $\log(5 \cdot 2) = \log 5 + \log 2$

3. $\log(5 - 2) = \log 5 - \log 2$ 4. $\log\left(\frac{5}{2}\right) = \log 5 - \log 2$

5. $\log(5 \cdot 2) = 2 \log 5$ 6. $\log\left(\frac{5}{2}\right) = \frac{\log 5}{\log 2}$

7. $\log(5^2) = \log 5 \cdot \log 5$ 8. $\log(5^2) = 2 \log 5$

9. $\ln(x+2) = \ln x + \ln 2$ 10. $\log(7x) = 7 \log x$

11. $\log(5x) = \log 5 + \log x$ 12. $\ln\left(\frac{x}{5}\right) = \ln x - \ln 5$

13. $\log\left(\frac{x}{4}\right) = \frac{\log x}{\log 4}$ 14. $\log_4 x^3 = 3 \log_4 x$

15. $\ln(x^2) = \ln x \cdot \ln x$ 16. $\log|4x| = \log 4 + \log|x|$